

**HW #21**

**1. Derivation for Exam 3:** Show that, for the 3D particle-in-a-box with energies given by

$$E = \frac{\pi^2 \hbar^2}{2mL^2} (n_x^2 + n_y^2 + n_z^2)$$

the density of states is  $g(E) = 8\pi\sqrt{2} \left(\frac{m}{\hbar^2}\right)^{3/2} E^{1/2}$

**2. Density of states in one and two dimensions.**

- a. Show that the density of states (number of states per unit length per unit energy) for a particle in a box in one dimension is

$$g_1(E) = \frac{1}{\pi} \left(\frac{2m}{\hbar^2 E}\right)^{1/2}$$

- b. Show that in two dimensions, the density of states (number of states per unit area per unit energy) is

$$g_2(E) = \frac{m}{\pi\hbar^2}$$

which is independent of  $E$ !

- c. Make a sketch of  $g_1$ ,  $g_2$ , and  $g_3$  (the three dimensional density of states) vs.  $E$ .

**3. (Kasap Example 4.7) Density of states in a band** Given that the width of an energy band is typically  $\sim 10\text{eV}$ , calculate the following, in per  $\text{cm}^3$  and per eV units:

- The density of states at the center of the band.
- The number of states per unit volume within a small energy range  $kT$  about the center.
- The density of states at  $kT$  above the bottom of the band.
- The number of states per unit volume within a small energy range  $kT$  to  $2kT$  from the bottom of the band.