For each vector pair below, sketch the pair and calculate $\vec{A} \cdot \vec{B}$.

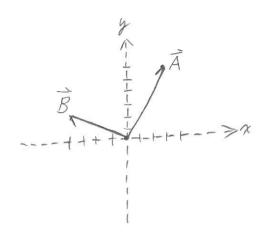
a.
$$\vec{A} = 3\hat{i} + 6\hat{j}$$

b. $|\vec{A}| = 2 \cdot \sqrt{10}, \theta = -71.6^{\circ}$
c. $\vec{A} = -5\hat{i} + 2\hat{j}$

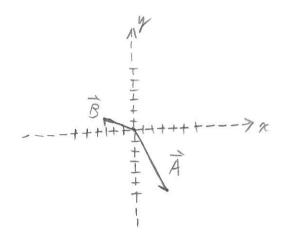
c.
$$\vec{A} = -5\hat{i} + 2\hat{j}$$

$$\vec{B} = -4\hat{i} + 2\hat{j}$$

$$B = -3i + 1j$$



$$\vec{A} \cdot \vec{B} = (-3.4 + 6.2) = 0$$

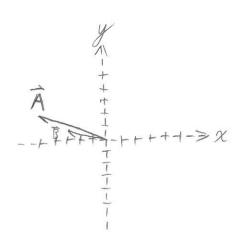


$$A_x = 2\sqrt{10'}\cos(-71.6) = 2.0$$

 $A_y = 2\sqrt{10'}\sin(-71.6) = -6.0$

$$\vec{A} \cdot \vec{B} = (2 \cdot 3 - 6 \cdot 1) = -12$$

(c)



 $\vec{A} \cdot \vec{B} = (+15 + 2) = 17$

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For each vector pair in the previous question, use your calculated dot product to find the angle θ between \vec{A} and \vec{B} .

and
$$\vec{B}$$
.

 $\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta \implies \theta = \cos^{-1} \left(\frac{\vec{A} \cdot \vec{B}}{|\vec{A}| |\vec{B}|} \right)$

a) $|\vec{A}| = (3^2 + 6^2)^2 = 6.7$, $|\vec{B}| = (4^2 + 3^2)^2 = 4.5$
 $\theta = \cos^{-1} \left(\frac{0}{67)(4.5} \right) = \boxed{90}$

b) $|\vec{A}| = 2\sqrt{10}$, $|\vec{B}| = (3^2 + 1^2)^{1/2} = \sqrt{10^4}$, $\theta = (0)^{-1/2} \left(\frac{-1/2}{2\sqrt{10}\sqrt{10}} \right) = 127^\circ$

c)
$$|\vec{A}| = (5^{\circ} + 2^{\circ})^{1/2} = 5.4, |\vec{B}| = (3^{\circ} + 1^{\circ})^{1/2} = 3.2$$

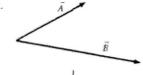
 $\Theta = (05^{\circ} \cdot (\frac{17}{(5.4)(32)}) = 10.3^{\circ}$

3. Which pairs of vectors are orthogonal? What is the dot product of the orthogonal pairs?

Pair a is orthogonal. When
$$\vec{A} \perp \vec{B}$$
, $\vec{A} \cdot \vec{B} = 0$

For each pair of vectors below, is the sign of $\vec{A} \cdot \vec{B}$ positive, negative or zero?

а



Sign = +

a



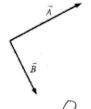
Sign =

b.



Sign = +

a



Sign =

C



Sign = ____

f.



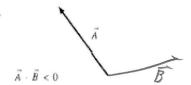
Sign =

Each of the diagrams below shows a vector \vec{A} . Draw and label a vector \vec{B} that will cause $\vec{A} \cdot \vec{B}$ to have the indicated sign.

n



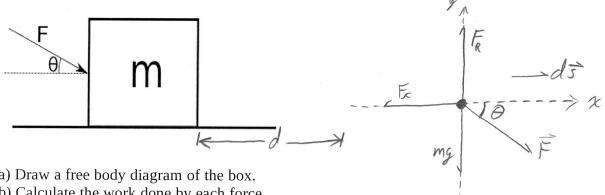
b



C



A box with mass *m*, initially at rest, is pushed a distance *d* along a surface with a force *F* making and angle θ with the horizontal. The coefficient of friction between the box and the surface is μ_k .



a) Draw a free body diagram of the box.

b) Calculate the work done by each force.

W=
$$\int \vec{F} \cdot d\vec{s}$$
, $d\vec{s} = dx A$
 $F_R: W = \int_{R}^{d} (F_R f) \cdot (dx A) \Rightarrow W = F_R(A f) \int_{R}^{d} dx \Rightarrow W = Q$
 $Mg: W = \int_{R}^{d} (-mgf) \cdot (dx A) = W = -mg(A f) \int_{R}^{d} dx \Rightarrow W = |F||A| \cos\theta \int_{R}^{d} dx$
 $W = \int_{R}^{d} (F) \cdot (dx A) \Rightarrow W = F \cdot A \int_{R}^{d} dx \Rightarrow W = |F||A| \cos\theta \int_{R}^{d} dx$
 $W = \int_{R}^{d} (F \cos\theta A + F \sin\theta A) \cdot (dx A)$
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Fx: W= (-Ex).(dxx) = - Ex.x (dx =) [w=-Ed]

From NSL, we Find the Frictional Force

NSL

y: FR - mg - FSINO = O

=) FR = Mg + FSINO => |FR = MK (Mg + FSINO) |

and WE= -UK (mg + FSINO)d

For each situation described below:

- a) Draw a free body diagram.
- b) Make a table next to each free body diagram showing each force and whether the work is positive, negative, or zero
- 1. An elevator being pulled upward by a cable.

2. The same elevator on the trip down.

3. A mover pushing a box across a rough floor.

$$F_{F}: -$$

$$F_{R}: 0, \vec{k}_{\perp} d\vec{s}$$

$$F_{P}: +$$

$$my: 0, m\vec{g}_{\perp} d\vec{s}$$

4. A ball thrown straight up. Consider the ball from the point just after it leaves your hand until the highest point in its trajectory.

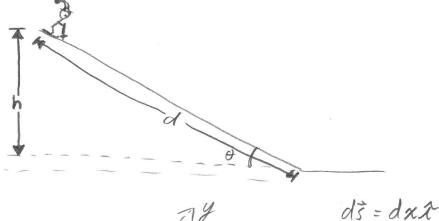
1 ds mg: - Gravity opposes ds

5. A mass on a string swings one revolution in a circle on a horizontal, frictionless table at a constant speed.

Filds Filo dil F

A skier of mass m skis a distance L down a frictionless hill that has a constant angle of inclination θ . The top of the hill is a vertical distance h above the bottom of the hill.

- a. Use the integral form of the definition of work to find an expression for the work done on the skier by each of the forces involved.
- b. Find an expression for the **total** work, W_{net} , done on the skier. Your expression should be in terms of m, g, and h only.



FR ds

 $W_{NET} = W_{F_R} + W_g$ = 0 + mg d sING $W_{NET} = mg h$

$$F_{R}: W_{R} = \int_{R} \tilde{F}_{R} \cdot d\vec{s} = \int_{0}^{R} (F_{R} \cdot \vec{J}) \cdot (dx \cdot \vec{x})$$

$$= F_{R} (\vec{J} \cdot \vec{A}) \int_{0}^{R} dx = O$$

$$mg: W_{g} = \int_{0}^{R} m\vec{g} \cdot d\vec{s}$$

$$= \int_{0}^{R} (mg SINOX + mg cosog) (dx \cdot \vec{x})$$

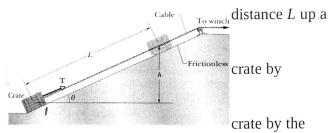
= $mg SIND(X.X) \int_{0}^{d} dx$

W = mgd SINA

Energy Problems - Set 1

An initially stationary crate of mass m is pulled a frictionless ramp to a height h where it stops.

a) Find an expression for the work W_g done on the gravity during the lift in terms of m, h, and g.



b) Find an expression for the work W_T done on the tension T in the cable during the lift in terms of m, h and g.

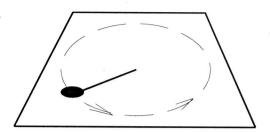
The state of the s

a)
$$W_g = \int m\vec{g} \cdot d\vec{s} = \int (-mg SINDA - mg cos \theta \vec{g}) (dx \vec{x})$$

$$= -mg SIND(\vec{x} \cdot \vec{x}) \int_{0}^{d} dx = mg L SIN \theta$$

$$W_g = -mgh$$

A particle of mass m moves in a horizontal circle of radius R on a rough table. It is attached to a string fixed at the center of the circle. The coefficient of friction between the mass and the table is μ_k .



- a) Draw a free body diagram of the puck.
- b) Calculate the work done by each force.
- c) Calculate the net work.

$$F_{R} = \int_{R}^{R} \left(-\frac{1}{4} \frac{1}{4} \frac{1}{4$$

Wnet = - MAMY 2TR