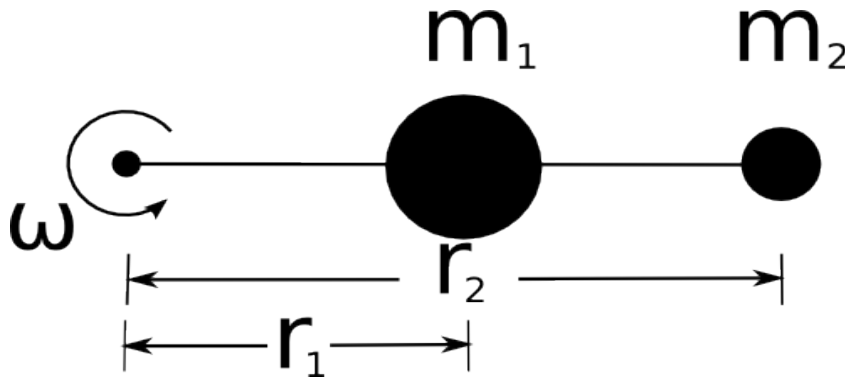


Consider a thin (essentially massless) bar with two masses attached to it as pictured below. The bar is rotating about the point shown in the diagram with an angular velocity  $\omega$ .



a) Write an expression for the total kinetic energy of the system in terms of  $r_1$ ,  $r_2$ , and  $\omega$ . Simplify your expression as much as possible.

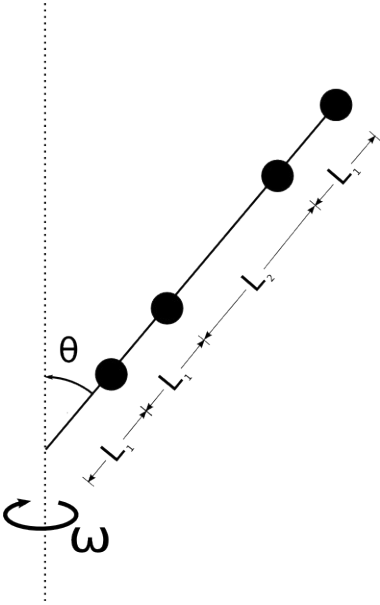
b) Generalize the expression above to a system with  $n$  masses (use a summation symbol,  $\Sigma$ , in your expression).

## Rotation – Set 2

2

Four point masses, each of mass  $m$ , are attached to a rigid massless rod that makes an angle  $\theta$  with the axis of rotation. Let  $L_2 = 2L_1$ .

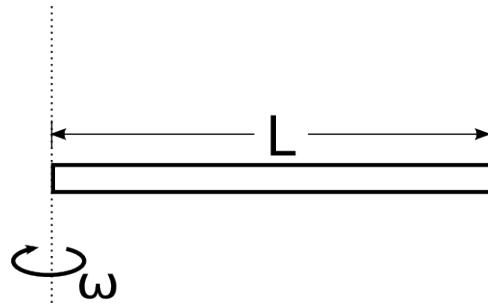
- What is the moment of inertia of this system?
- What is the kinetic energy of this system if it's rotating with angular velocity  $\omega$ .



## Rotation – Set 2

3

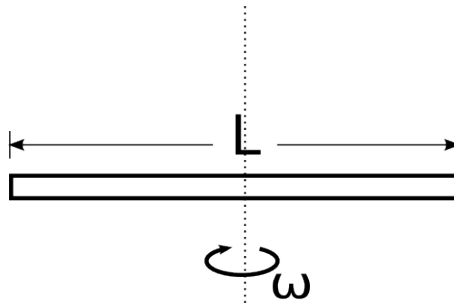
Calculate the moment of inertia of a uniform bar of length  $L$  and mass  $M$  about the axis of rotation shown.



## Rotation – Set 2

4

Calculate the moment of inertia of a uniform bar of length  $L$  and mass  $M$  about the axis of rotation shown.

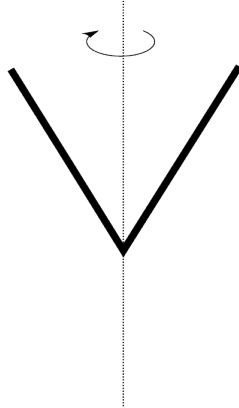




## Rotation – Set 2

6

Calculate the moment of inertia of the bent rod of mass  $M$  shown in the figure below. The rotation axis is in the plane of the "V" bisecting it at the vertex. The rod is bent at an angle  $\theta$  and each leg has a length  $L$ .



## Rotation – Set 2

7

A thin rod of length  $L$  has a non-uniform density profile of  $\lambda = \lambda_0 \left[ 2 \frac{l^2}{L^2} + \frac{1}{3} \right]$ .

What is the moment of inertia of this rod if it's about an axis perpendicular to the light end of the rod? Write it in terms of the total mass  $M$ .

HINT: Integrate to get the total mass and then integrate to get the moment of inertia and combine the two results.