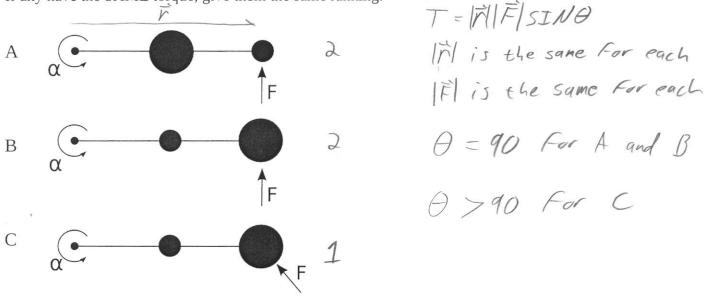
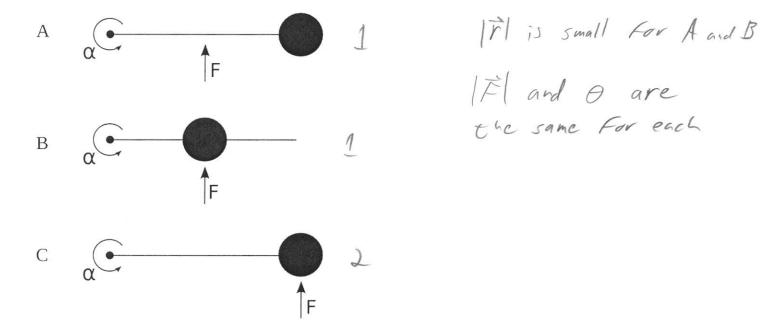
In the pictures below, two masses are connected by a massless rod and the system is allowed to rotate about the pivot shown. The large circle is more massive than the small circle. A force is applied to each system as shown in the diagram.

Rank the three systems in order of the applied *torque*, least to most. **Explain your reasoning.** 

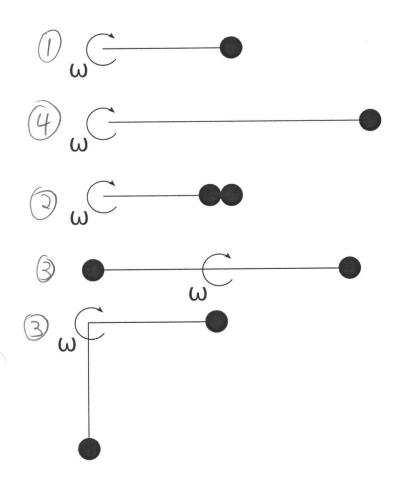
If any have the SAME torque, give them the same ranking.



Rank the three systems in order of the applied *torque*, least to most. **Explain your reasoning.** If any have the SAME torque, give them the same ranking.



Below are several objects. Each circle is a point mass, and each point has the same mass. The connecting rods are massless. Rank them in order of moment of inertia, least to most. If any have the SAME moment, give them the same ranking number. **Explain your reasoning**.



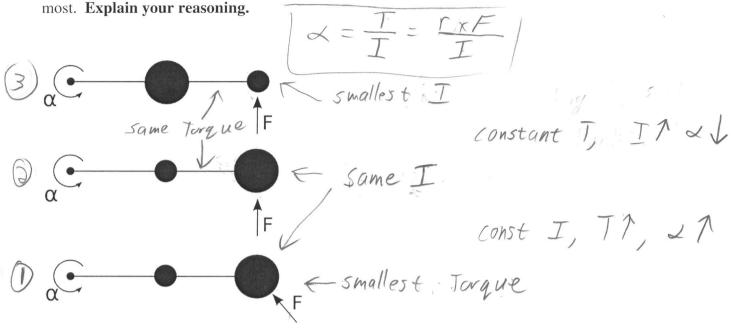
I = \( \int\_{i}^{\gamma^{2}} \), so: The top object has a single mass

next, 2 < 3 because the mass doubles but 2 has one mass sightly closer to the pivot

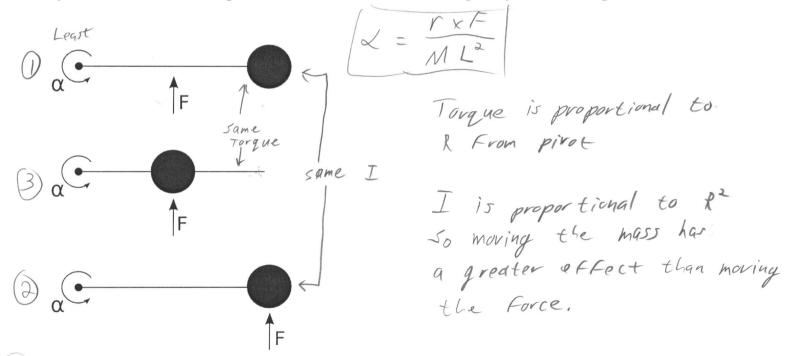
the 2 3's have twice the mass, but both at the same distance

last 4 is a single mass twice as Far but I gets as p2 so r makes a UST Physics, A. Green, M. Johnston and G. Ruch bigger difference than M.

In the pictures below, two masses are connected by a massless rod and the system is allowed to rotate about the pivot shown. The large circle is more massive than the small circle. A force is applied to each system as shown in the diagram. Rank the three systems in order of their angular accelerations, least to



In the pictures below, two masses are connected by a massless rod and the system is allowed to rotate about the pivot shown. A force is applied to each system as shown in the diagram. Rank the three systems in order of their angular accelerations, least to most. **Explain your reasoning.** 



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A small 0.75 kg ball is attached to one end of a 1.25 m long massless rod. The other end of the rod is hung from a pivot under the influence of gravity. When the resulting pendulum is  $30^{\circ}$  from vertical:

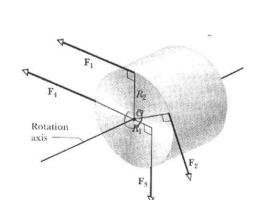
- a) What is the magnitude of the torque about the pivot? (Draw a free body diagram)
- b) What is the instantaneous angular acceleration (the acceleration at the moment when the pendulum is released)?
- c) Can we use kinematics to find the angular velocity of the pendulum at the bottom of its swing? Why or why not?  $a) \overrightarrow{T} = \overrightarrow{L} \times \overrightarrow{F} = (1.25)(9.8) \times 10^{-10} \times$



a) 
$$T = I \lambda \Rightarrow \lambda = \frac{T}{I} = \frac{4.6}{(0.75)(1.25)^3} = 3.9 \text{ rad/s}$$

c) No, because the tarque is not constant. It depends on the angle of

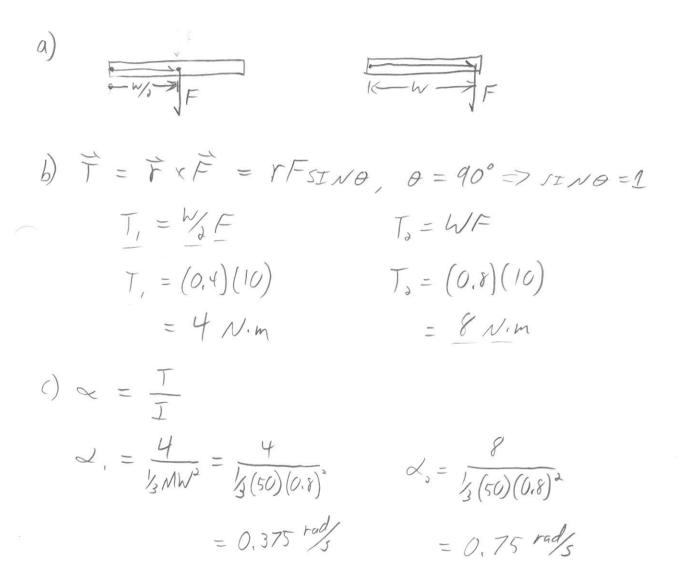
A cylinder with a mass of 2.0 kg can rotate about its central axis through the point 0. Forces are applied as in the figure below.  $F_1 = 6.0 \text{ N}$ ,  $F_2 = 4.0 \text{ N}$ ,  $F_3 = 2.0 \text{ N}$ ,  $F_4 = 5.0 \text{ N}$ . Find the direction and the magnitude of the angular acceleration of the cylinder. (During rotation, the forces maintain the same angles relative to the cylinder.)  $R_3 = R_1 = 0.05 \text{ m}$ 



$$V = \frac{1}{\sqrt{(2)(1)^2}} [(60)(.12) - (40)(.12) - (2.0)(.05)] = 9.7 \text{ rad/s}$$

A door has a mass of 50 kg and is 0.8 m wide. The moment of inertia is I = 1/3 MW<sup>2</sup> where W is the width of the door. I push on the door with a constant force of F = 10 N in two places; in the middle of the door a distance W/2 from the hinge and at the knob, a distance W from the hinge.

- a) Draw free body diagrams of the two cases.
- b) What is the magnitude of the Torque for each case?
- c) What is the magnitude of the angular accelerations for each case?
- d) How much time does it take the door to rotate through 90° in each case?
- e) How much force would I have to apply at W/2 so that the door rotated through 90° in the same amount of time as applying 10 N to the knob?



d) 
$$\theta = 9 + 4 + 4 \times t^2$$

$$\theta = 4 \times t^2 \implies t = \left(\frac{2\theta}{\alpha}\right)^{\frac{1}{2}}, \quad t_1 = \left(\frac{(2)(\frac{1}{2})}{0.375}\right)^{\frac{1}{2}} = 2.9 \text{ s}$$

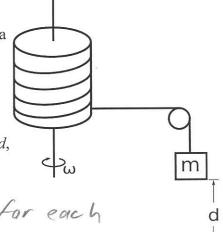
$$t_2 = \left(\frac{27}{0.75}\right)^{\frac{1}{2}} = 2.0 \text{ s}$$

## Rotation - Set 4

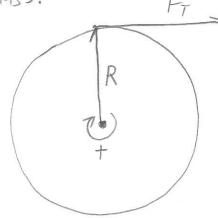
A solid cylinder of mass M, radius R, and moment of inertia  $I = \frac{1}{2}MR^2$  is allowed to rotate without friction about an axis through its center as shown. A massless string is wrapped around the cylinder, passes over a small massless frictionless pulley and is attached to a small mass m.

If the mass and the cylinder start from rest, what will the angular velocity of the cylinder be after the mass falls through a distance d?

Using **Torque and Kinematics**, find an expression for  $\omega_f$  in terms of d, M, m, and R.



1) Draw Free-Body Diagrams, one for each mass.



Cylinder, Top View Defining clockwise rotation as positive. Defining down

From as positive y

to agree with

mag positive rotation

of the cylinder

2) Write Newton's 2nd law, Both torque version and translation version For each mass.

Cylinder, torque only hotranslation

ラデェエム

> R.FSIND = IL

Hanging mass, translation only

ZF=M9

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continued 1

Rotation Set 4, P7 Continued

Cylinder

ZRFSINO = IX 0 = 90°, SINO = 1

= JRF = IL, I=BMR

=>RF=LMR2

=> FT = & MRX O

Hanging mass

ZF=ma

[mg-F,=ma]

Combine 0 and 0 to eliminate  $F_T$ , solve  $F_{0T} \propto mg - \frac{1}{2}MR \propto = m.a$ ,  $a = R \propto$ 

=> mg - &MR& = mR&

= mg = (/M+m) RX

 $= )3) = \frac{m}{2M + m} \frac{g}{R}$ 

save this for later.

3) We have acceleration. Now we need to use kinematics to get a, the angular Velocity.

 $\theta = 90 + 400 + 4$ 

 $\theta = 1 \times \frac{\omega^2}{\omega^2} \Rightarrow \left[\omega = \left[2\theta\omega\right]^2\right]$ 

 $\omega = 0$  t = 0 t = 0 t = 0

continued

Rotation Set 9, P7 continued

so we have: W=[202] 2

we are given d, so we need to write  $d=R\Theta$ =>\O =  $\frac{d}{R}$ 

Then: W=[2 R 2]2

And we plug in & From eq. (3)

$$\omega = \left[ \frac{m}{3M + m} \frac{2dg}{R^2} \right]^{\frac{1}{2}}$$

## Rotation - Set 5

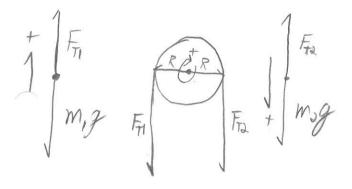
Use Torque and Kinematics to solve the following problem.

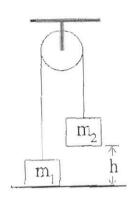
Two masses are connected by a light string passing over a frictionless pulley. the Mass  $m_2$  is released from rest at a height of 4.0 m above the ground. You can treat the pulley as a solid disk.

Determine the speed of m<sub>1</sub> as m<sub>2</sub> hits the ground.

$$\begin{split} m_1 &= 3.0 \text{ kg} \\ m_2 &= 5.0 \text{ kg} \\ m_{\text{pulley}} &= 0.5 \text{ kg} \\ r_{\text{pulley}} &= 0.1 \text{ m} \end{split}$$

$$r_{\text{pulley}} = 0.1 \text{ r}$$





Force  

$$F_{\pi_1} - M_1 g = M_1 Q O$$
  
 $M_1 g - F_{\pi_2} = M_2 Q O$ 

continued

$$Rm_{\alpha}(g-a)-Rm_{\alpha}(a+g)=I_{\alpha}$$

Want a For kinematics, so sub  $2 = \frac{a}{R}$ and sub I = 2 m, R2

=> 
$$Rm_s(g-a)-Rm_s(a+g)=sm_pR\frac{a}{R}$$

$$\Rightarrow$$
  $(m_s - m_s)g = (m_s + m_s + 3m_p)a$ 

$$= \int a = \frac{m_2 - m_1}{m_1 + m_2 + l_2 m_p} g$$

\* Do kinematics, sub in a last

$$=> V = (\partial ya)^{1/2} =>$$

$$\Rightarrow t = \frac{v}{q}$$