Systems of Particles - Set 3

A HUGE truck, T and a Prius, P, move towards each other, collide and stick. Let \mathbf{F}_p be the force experienced by the Prius and let \mathbf{F}_T be the force experienced by truck.



- 1. \mathbf{F}_{P} is ____ \mathbf{F}_{B} .
 - a) Greater than
 - (b) The same as
 - c) Less than

Newton's 3rd Law

2. The amount of time that \mathbf{F}_P is applied is _____ the time that \mathbf{F}_T is applied.

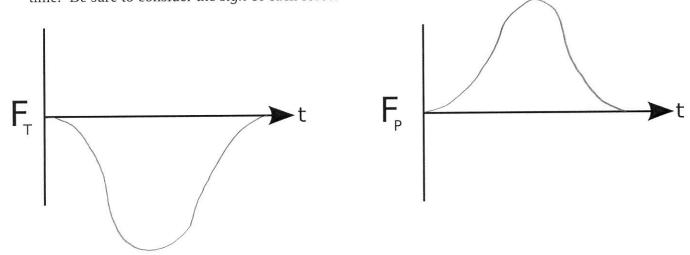
- a) Greater than
- b) The same as

c) Less than

It's a contact force --.

One can't lose contact before
the other.

3. Sketch a graph showing a plausible \mathbf{F}_P as a function of time and another graph showing \mathbf{F}_T function of time. Be sure to consider the *sign* of each force.



Forces are equal and opposite.

5. Compare the impulses on the two. What's the same? What's different? $\vec{J} = \vec{F} dt = \Delta \vec{p}$ Because the Force and the time are the same, magnitude the impulse must also have the same magnitude.

The Forces are oppisitely directed, so the impluse is also.

- 4. The *magnitude* of the change in momentum of the Prius is ____ the *magnitude* of the change in momentum of the truck.
 - a) Greater than

(b) The same as

c) Less than

5. The magnitude of the acceleration of the Prius is _____ the magnitude of the acceleration of the truck.

a) Greater than

b) The same as

c) Less than

and
$$\vec{F} = m\vec{a}$$
.

You are in a car accident in which you collide with a concrete wall at 30 mi/hr. You are not wearing your seat belt and stop yourself using the reaction force of the windshield against your head. Let's assume that you don't go through the window.

a) What is the average force on your head, assuming the impact lasts 0.01 seconds. Compare that force to the weight of a person. (the *mass* of a person is about 70 kg, what's their weight?)

$$F_{AVG} = \frac{\Delta P}{\Delta t}, \quad P_{F} = 0, \quad P_{I} = 30 \text{ m/s} \cdot 1.61 \times 10^{3} \text{ m/s} \cdot \frac{1}{3600} \text{ m/s} \cdot 70 \text{ kg} = 939 \text{ kg/ms}$$

$$F_{AVG} = \frac{939 \text{ kg/ms}}{0.01 \text{ s}} = \boxed{4.39 \times 10^{4} \text{ N}} \quad \frac{F_{AVG}}{V_{P}} = \frac{9.39 \times 10^{4} \text{ N}}{70 \text{ kg} \cdot 9.8 \text{ m/s}} = 137 \text{ people}$$
on your hand

b) Now, you're wearing your seatbelt so you get to take advantage of the car's crumple zones. Crumple zones cause the impact to take place over 0.1 seconds. NOW what's the average force?

A 4000 kg railroad car collides and sticks to a chain of three other 4000 kg cars initially sitting at rest on a rough track. The four cars travel together down the rough track for 1.5 m before they stop. Assuming $\mu_k = 0.10$, what is the velocity of the first car at impact?

Answer these important questions before "solving" this problem:

Does the train car conserve momentum throughout the entire problem? Why not?

Is there a sub-problem where conservation of momentum can be applied? What is it?

What other physics principal are you going to use to solve the problem?

Draw a picture (or pictures) showing the action.



Do the math and solve the problem. Q conserve Energy

(1) Collide

$$k_{\perp} = 54mV_{e}^{2} \quad k_{\perp} = 0, \quad w_{\perp} = -u_{e} + u_{g} d$$
 $k_{\perp} = 4mV_{e}^{2} \quad k_{\perp} = u_{e} + u_{g} d$
 $V_{\perp} = 4V_{e} \quad V_{\perp} = (32 \, M_{e} \, g \, d)^{3}$
 $V_{\perp} = (32 \, M_{e} \, g \, d)^{3}$

 $V_{+} = (32(0.1)(9.8)(1.5))^{1/2} = [6.9 \text{ m}]$

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You are driving West along Summit Ave, lawfully doing the speed limit (50 km/hr) in your new car which (as you've read in the owners manual) has a mass of 1500 kg. Sleepy McSnoozer is driving South along Cleveland in his 1965 Ford pickup truck loaded with bags of cement. His truck (plus cement) weighs 2300 kg. Sleepy runs the red light and smashes into your car. The cars fuse together and skid to a stop.

Certain that Sleepy was speeding, you measure the skid mark and find that the length of the skid is L = 18 m. You look up the rubber/asphalt coefficient of friction and find that it is $\mu_k = 0.6$.

What was Sleepy's velocity? Was he speeding? The speed limit is 50 km/hr.

$$M_{\kappa} = 0.6$$

 $L = 18$
 $M_{\star} = 1500 \, \text{kg}$
 $M_{\star} = 2300 \, \text{kg}$
 $M_{\star} = 50 \, \text{km/m} \cdot 1 \times 10^{3} \, \text{m/m} \cdot \frac{1}{3600} \cdot \frac{\text{kr}}{\text{s}} = 13.9 \, \text{m/s}$

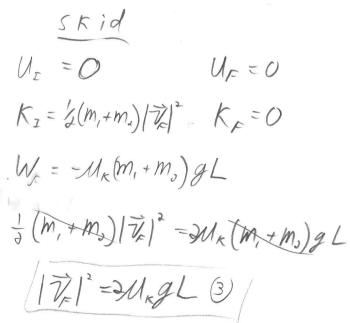
Two parts, collision and skid. Conserve momentum For collision, Conserve energy to do skid.

Collision
$$P_{I} = P_{F}$$

$$\chi: m_{1}V_{1} = (m_{1} + m_{3}) V_{FX}$$

$$y: m_{2}V_{2} = (m_{1} + m_{3}) V_{FY}$$

$$0 V_{FX} = \frac{m_{1}}{(m_{1} + m_{3})} V_{1}, \quad 0 V_{Y} = \frac{m_{2}}{(m_{1} + m_{3})} V_{2}$$



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continued &

Systems of particles Set 3, P3 continued

Now: $|\vec{V}_F|^2$ is related to V_{EX} and V_{EY} by pythagoras. $|\vec{V}_F|^2 = V_{EX}^2 + V_{EY}^2$

Plugging @ > 3:

5 Vex + Vey = 2 MrgL

and plugging Dand 6 > 6

 $\frac{m_{1}^{2}}{(m_{1}+m_{3})^{3}}V_{1}^{2}+\frac{m_{3}^{2}}{(m_{1}+m_{3})^{*}}V_{3}^{2}=2M_{K}gL$

and solve For Vii

m, V, + m, V, = 2 Mrg L

m; V, + m, V, = 2 Magl (m, + m2)

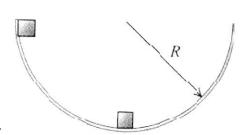
 $=) \left[\mathcal{V}_{s} = \left[2 \mathcal{U}_{k} \mathcal{G} L \left(m_{s} + m_{s} \right)^{2} - m_{s}^{2} \mathcal{V}_{s}^{2} \right] \frac{1}{m_{s}} \right]$

 $V_{\delta} = [(2)(0.6)(9.8)(18)(1500 + 2300)^{2} - (1500 \cdot 13.9)^{2}]^{\frac{1}{2}} \frac{1}{2300}$

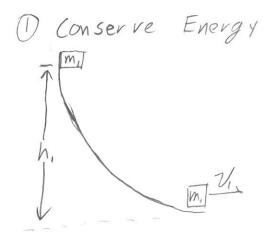
 $V_3 = 22.3 \% \cdot 1 \times 10^{-3} \frac{\text{km}}{\text{m}} \cdot 3600 \% = 80 \text{ km/hr}$

Speeder!

Two masses, m_1 and m_2 , are released from rest in a frictionless hemispherical bowl of radius R from the positions shown in the figure. The upper mass collides with and sticks to the lower mass and the two slide up the other side together.



Derive an expression for their final height of the combined masses.



$$U_{I}=m,gh, \qquad U_{F}=0$$

$$K_{I}=0 \qquad K_{F}=2m,V_{i}^{2}$$

$$M_{i}gh_{i}=2m,V_{i}^{2}$$

$$V_{i}=\sqrt{2gh_{i}}$$

$$m_{1}V_{1} + m_{2}(0) = (m_{1} + m_{2})V_{2}$$

$$V_{2} = \frac{m_{1}}{(m_{1} + m_{2})}V_{1}(2)$$

$$U_{I} = 0 \qquad U_{F} = (m_{1} + m_{2})gh_{2}$$

$$K_{I} = \delta(m_{1} + m_{2})V_{0}^{2} \qquad K_{F} = 0$$

$$= \sum_{h_{2}} \left[\frac{V_{2}^{2}}{2g} \right] (3)$$

Systems of Particles Set 3, P6 continued.

From 3:
$$h_2 = \frac{V_3^2}{2g}$$

Plug in 2: $h_3 = \frac{1}{3g} \left[\frac{m_1}{m_1 + m_2} \right]^2 V_4^2$

Plug in 0: $h_3 = \frac{1}{3g} \left[\frac{m_1}{m_1 + m_2} \right]^2 2gh_1$
 $h_4 = \left[\frac{m_1}{m_1 + m_2} \right]^2 h_1$

MOMENTUM, IMPULSE, AND COLLISIONS

1. A large fish will soon make a dish of a smaller fish. What is the velocity of the large fish and his dinner immediately after he eats? Give both the magnitude and direction of the final velocity with respect to the x-axis.

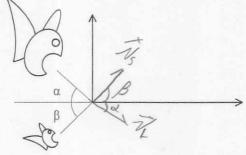
m
$$_{large\ fish} = 4.0\ kg$$

 $v_{o\ large\ fish} = 1.0\ m/s$
 $\alpha_{large\ fish} = 25.0^{\circ}$

$$m_{small\ fish} = 0.20\ kg$$

$$v_{o\ small\ fish} = 5.0\ m/s$$

$$\beta_{small\ fish} = 50.0^{\circ}$$



Conserve momentum in both axis

$$\alpha : M_L \chi_{COS} + M_S V_S \cos \beta = (M_L + M_S) \chi_{COS} \theta$$

Divide y by x to eliminate Vx

$$\theta = tan' \left[\frac{(4.0)(1.0)StN(25) + (0.2)(5)SIN(50)}{(4.0)(1.0)COS(25) + (0.2)(5)COS(50)} = \left[-12^{\circ} \right] \right]$$

Plug back into x (or y) to get V

$$V_{F} = \frac{m_{L}V_{L}(OS2 + m_{S}V_{S}(OSB)}{(m_{L} + m_{S})COS\theta} = \frac{(4)(1)(OS25 + (0.2)(5)COS(50)}{(4 + 0.2)(COS(-12))} = 1.0 \frac{m_{S}}{5}$$