



Neo and Agent Smith are flying towards each other. They collide in mid air and grab onto each other (they stick together).

a) Assume that momentum is conserved in the Matrix and find an expression relating their initial velocities to their final velocity.

b) Let  $M_N = 70$  kg,  $V_{Ni} = 50$  m/s,  $M_S = 100$  kg, and  $V_{Si} = 35$  m/s. Put these numbers into your expression and solve for their final velocity.

c) Calculate the pre-collision and post-collision kinetic energy of the system. Does this system conserve kinetic energy through the collision?

## Systems of Particles – Set 4

2

Gayle runs at a speed of 4.0 m/s and dives onto a sled that is initially at rest on top of a frictionless snow covered hill sloping down at  $30^\circ$ . After she has traveled 10 m down the slope, her brother Billy hops on the sled; What is their speed after Billy hops on?

$$m_{\text{Gayle}} = 50.0 \text{ kg}, m_{\text{Billy}} = 30.0 \text{ kg}, m_{\text{sled}} = 5.0 \text{ kg}$$

## Systems of Particles – Set 4

3

Gayle, whose mass is  $m_G$ , is running at a speed  $V_0$  towards her sled, which is initially at rest and has a mass  $m_s$ . Gayle jumps on the sled. Find the velocity,  $V_1$ , of Gayle and her sled after the “collision.”

This system **conserves momentum** through the collision. Write a sentence that your grandmother would understand explaining what it means to conserve momentum.

- a) Draw a before and after picture representing the collision. Label all appropriate masses and velocities.
- b) Directly under each picture, write the total momentum of the system.
- c) Using this information, find an expression that relates  $V_0$  and  $V_1$ .

## Systems of Particles – Set 4

4

Gayle, whose mass is  $m_G$ , is riding on a sled, mass  $m_s$ , with an initial velocity  $V_1$ . She slides a distance  $d$  down a frictionless slope that makes an angle  $\theta$  with the horizontal. Find the the velocity,  $V_2$ , of Gayle and her sled after sliding a distance  $d$ .

This system **conserves energy**. Write a sentence that your grandmother would understand explaining what it means to conserve energy.

- a) Draw a before and after picture representing the action. Label all appropriate masses and velocities.
- b) Directly under each picture, write an expression for the the total energy of the system.
- c) Using this information, find an expression that relates  $V_1$  and  $V_2$ .

## Systems of Particles – Set 4

5

Gayle, whose mass is  $m_G$ , is riding on her sled, mass  $m_s$ , at a speed  $V_2$ . Her brother Bert, mass  $m_B$ , jumps on the sled. Find the velocity,  $V_3$ , of the Gayle plus Sled plus Bert combination after the “collision.”

This system **conserves momentum** through the collision. Write a sentence that your grandmother would understand explaining what it means to conserve momentum.

- a) Draw a before and after picture representing the collision. Label all appropriate masses and velocities.
- b) Directly under each picture, write the total momentum of the system.
- c) Using this information, find an expression that relates  $V_2$  and  $V_3$ .

## Systems of Particles – Set 4

6

A block with a mass of  $m_1 = 3.5$  kg is placed in front of a spring with spring constant  $k = 2.4 \times 10^4$  N/m that has been compressed a distance  $d$ . After the spring is released, the block slides without friction to a hanging pendulum. The block then slides into a cup with mass  $m_2 = 5$  kg. The cup is hanging from a string with length  $l = 1.4$  m. After the collision, the resulting pendulum swings up and makes a maximum angle  $\theta = 26.5^\circ$ .

What was the original spring compression  $d$ ?

