

Oscillation – Set 3

1

An oscillating block-spring system has a mechanical energy of 1.00 J, an amplitude of 10.0 cm, and a maximum speed of 1.20 m/s.

- a) What is the spring constant?
- b) What is the mass of the block?
- c) What is the frequency of oscillation?

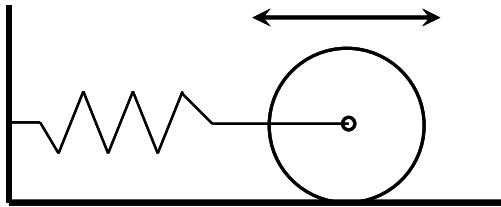
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2

Use **ENERGY** techniques to answer the following question.

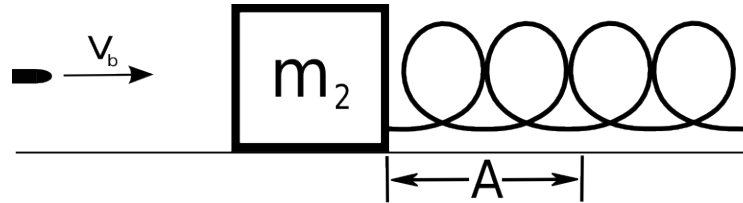
A solid cylinder of mass $M=2$ kg and radius $R=1.0$ m is attached to a horizontal spring with spring constant $k=100$ N/m. The cylinder can roll without slipping along the horizontal plane. When the system is displaced from the equilibrium position, it executes simple harmonic motion.

- Derive an expression for the period of the oscillations in terms of M and k .
- If the cylinder has a translational velocity of $v_0=5.0$ m/s as it passes through equilibrium, find the phase constant, the amplitude, and the maximum acceleration of the system.



A block of mass $m_2 = 10$ kg attached to a spring with spring constant $k = 5$ N/m is oscillating with an amplitude of $A = 1.5$ m horizontally on a frictionless surface. When the spring has reached its maximum extension to the left, it collides with a bullet with a mass $m_1 = 5$ g moving $V_b = 200$ m/s towards the right.

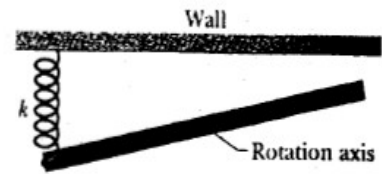
- a) What is the period of the oscillator after the collision?
- b) What is the amplitude of the oscillator after the collision?



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4

A long uniform rod of length L and mass m is free to rotate in a *horizontal* plane about a vertical axis through its center (the picture shows a *top* view). A spring with force constant k is connected horizontally between one end of the rod and a fixed wall. When the rod is in equilibrium, it is parallel to the wall.



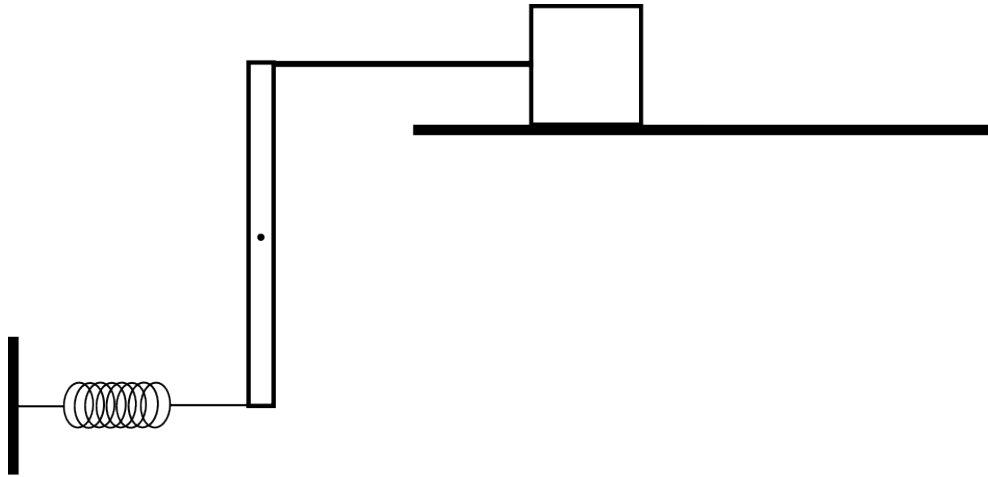
What is the period of the *small* oscillations that result when the rod is rotated slightly and then released?

$$I_{cm} = \frac{1}{12}ML^2 \text{ for the rod.}$$

- Use **Newton's Second Law** to find the oscillator frequency.
- Use **Energy Techniques** to find the oscillator frequency.

Use **ENERGY** techniques to answer the following question.

A block of mass M resting on a frictionless surface is attached to a stiff rod of negligible mass. The other end of the rod is attached to the top of a thin bar of length l mass M that is allowed to rotate about its center. The bottom of a bar is attached to a light spring of spring constant k . The spring is relaxed when the bar is vertical. Find the frequency of small oscillations.



Two particles are in simple harmonic motion in a straight line. They have the same amplitude and a period of 1.5 s but differ in phase by $\pi/6$ radians.

- a) How far apart are they from one another (in terms of A) when the lagging particle is at its maximum position?
- b) Are they moving in the same direction or opposite directions?
- c) How far apart are they 0.5 seconds later?
- d) Are they moving in the same or opposite directions then?