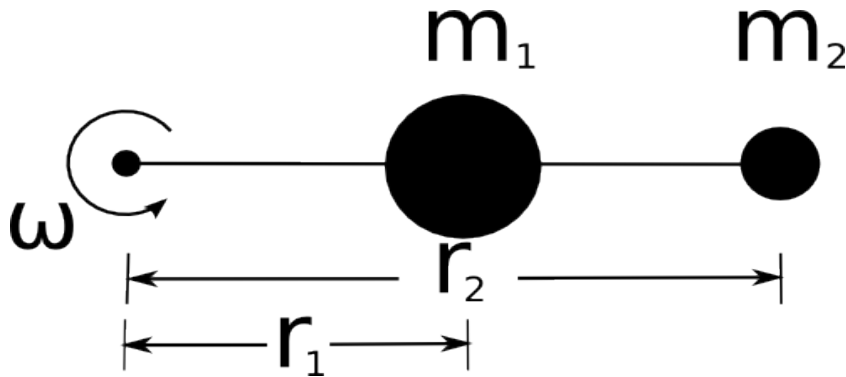


## Rotation – Set 2

1

Consider a thin (essentially massless) bar with two masses attached to it as pictured below. The bar is rotating about the point shown in the diagram with an angular velocity  $\omega$ .



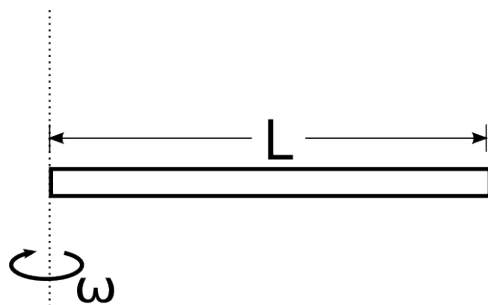
a) Write an expression for the total kinetic energy of the system in terms of  $r_1$ ,  $r_2$ , and  $\omega$ . Simplify your expression as much as possible.

b) Generalize the expression above to a system with  $n$  masses (use a summation symbol,  $\Sigma$ , in your expression).

## Rotation – Set 2

2

Calculate the moment of inertia of a uniform bar of length  $L$  and mass  $M$  about the axis of rotation shown.

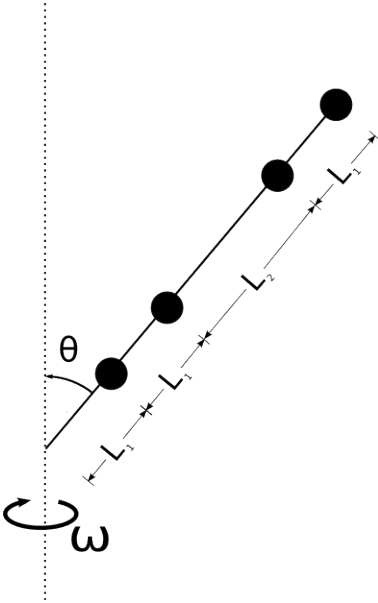


## Rotation – Set 2

3

Four point masses, each of mass  $m$ , are attached to a rigid massless rod that makes an angle  $\theta$  with the axis of rotation. Let  $L_2 = 2L_1$ .

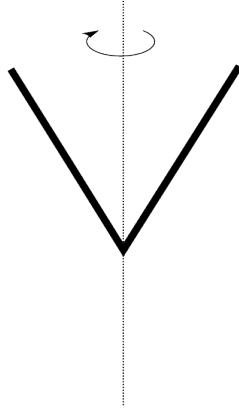
- What is the moment of inertia of this system?
- What is the kinetic energy of this system if it's rotating with angular velocity  $\omega$ .



## Rotation – Set 2

4

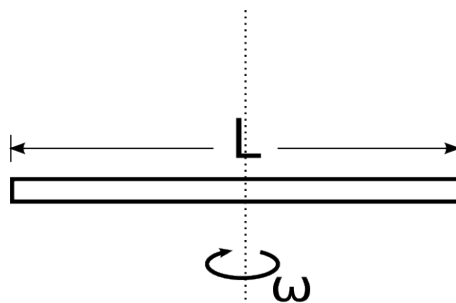
Calculate the moment of inertia of the bent rod of mass  $M$  shown in the figure below. The rotation axis is in the plane of the "V" bisecting it at the vertex. The rod is bent at an angle  $\theta$  and each leg has a length  $L$ .



## Rotation – Set 2

5

Calculate the moment of inertia of a uniform bar of length  $L$  and mass  $M$  about the axis of rotation shown.



## Rotation – Set 2

A thin rod of mass  $M$  has been bent into a semi-circle with radius  $R$ .

- Calculate its center of mass
- Calculate its moment of inertia about an axis through the center of mass perpendicular to the page.
- Calculate its moment of inertia about an axis in the plane of the page through the center of mass that vertically bisects the semi-circle.

