

## Rotation – Set 1

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An aging hippie is jammin' to his old "In-A-Gadda-Da-Vida" album. The turntable spins the record with a constant angular velocity  $\omega=33.33$  revolutions per minute. The hippie notices that when he turns off the turntable motor, the record makes exactly three revolutions before stopping.

- a) What's the angular deceleration of the record, man? (Assume it's a constant.)
- b) He also notices that when he starts the turntable, it takes the record 3.0 seconds to come up to speed. After the record gets up to speed, "In-A-Gadda-Da-Vida" plays for an agonizing 3.50 minutes. What is the total angular displacement of the record at the end of the song?



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Your hippie friend is fascinated by watching a quarter on his record go around and around and around. He's somehow managed to formulate a few questions about the quarter that he needs your help answering.



a) So dude, like, if I totally put the quarter a distance  $r$  from the center, like, what distance,  $c$ , does it go in one revolution?

b) Groovy, so then, like, how far does the quarter go, let's call the distance  $s$ , if the record rotates through an angle  $\theta$ .

c) Woah! Trippy... so then how FAST, is the quarter moving, call it  $v$ , in terms of the angular velocity  $\omega$ ?

d) Right on! So like, let's say the record totally has angular acceleration,  $\alpha$ ! What's the *tangential* acceleration,  $a_T$ , of the quarter?

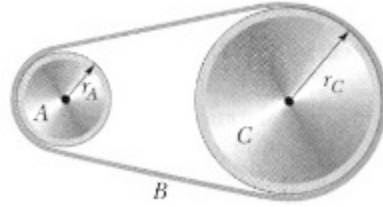
The hippie wants to explore rolling the record across the floor now. Thankfully, this means that the terrible music has stopped playing. Assume that the record rolls in a perfectly straight line.

- a) If the radius of the record is  $r = 30$  cm, how far has it rolled after one revolution?
- b) What is its total angular displacement after it has rolled 5 meters?
- c) If the initial *translational* velocity of the center of the record is 2 m/s, what is its angular velocity?
- d) If the record comes to a stop after 5 m, what was its *angular* acceleration (assuming constant acceleration).

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A pulley of radius  $r_A = 10$  cm is coupled by a belt to a pulley of radius  $r_C = 25$  cm. A motor is attached to the axle of pulley  $A$  giving it an angular acceleration of  $\alpha_A = 1.6$  rad/s<sup>2</sup>. How long does it take pulley  $C$  to achieve an angular velocity  $\omega = 100$  rev/min assuming that the belt does not slip?



A car's odometer works by counting the revolutions of the axle. A car's speedometer works by measuring the angular velocity of the axle. For the odometer and speedometer to work correctly, the correct tire radius has to be set at the factory.

My car came from the factory with tires with a diameter of  $d_1 = 60$  cm. They wore out and I replaced them with tires with a diameter of  $d_2 = 80$  cm.

a) With the proper tires on the car:

What is the angular displacement,  $\theta$ , (in radians and revolutions) of the tire after 1.0 km?

What is the angular velocity of the axle,  $\omega$ , (in rad/sec and rev/sec) if I'm driving 100 km/hr?

b) What are the answers to the questions in part a with the improper tires on the car?

c) If I've added 10,000 km to the odometer since putting the new tires on, how many km have I actually driven the car? (HINT: The odometer *assumes* that the proper tires are on the car.)

d) If the speed limit is 100 km/h, what should my speedometer read so that I don't get a speeding ticket? (HINT: The speedometer *assumes* that the proper tires are on the car.)

A diver makes 2.5 complete revolutions on the way from a 10 m high platform to the water. Assume that her initial vertical velocity was zero. What was her angular velocity, assuming that it was constant throughout the trip.

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A wagon wheel with a radius of 30 cm with 8 equally spaced spokes is spinning with an angular velocity of 2.5 revolutions/sec. You want to shoot a 20 cm arrow parallel to the wheel's axle between the spokes without hitting one. Assuming that the spokes and the arrow are very thin:

- a) What minimum speed must the arrow have?
- b) Does it matter where between the axle and the rim you aim? If so, where is the best location?