Rotation - Set 1

An aging hippie is jammin' to his old "In-A-Gadda-Da-Vida" album. The turntable on which the record sits spins it with a constant angular speed of 33.33 revolutions per minute. The hippie notices that when he turns off the turntable motor, the record makes exactly three revolutions before stopping.

- a) What's the angular deceleration of the record in radians per second, man? (Assume it's a constant.)
- b) He also notices that when he starts the turntable, it takes the record 3.0 seconds to come up to speed. After the record gets up to speed, "In-A-Gadda-Da-Vida" plays for an agonizing 3.50 minutes. What is the total angular displacement of the record at the end of the song?





$$\Theta_0 = 0$$

$$Q = 3 \text{ rev}$$

$$Q = 33.3 \text{ rev}_{\text{min}} = 33.3 \text{ rev}_{\text{min}} \cdot \frac{1}{60} \frac{\text{min}}{5} = 0.55 \text{ rev}_{\text{s}}$$

$$Q = 0$$

$$\theta = \theta_0 + \omega_0 t + \zeta_2 t^2$$

$$\theta = \omega_0 t + \zeta_2 t^2$$

$$\omega = \omega_0 + zt$$

$$\theta = -\frac{\omega_o^2}{\omega} + \frac{1}{2} \times \frac{\omega_o^2}{\omega^2}$$

$$=$$
 $t = -\frac{\omega_0}{\lambda}$

$$\theta = -\frac{1}{2}\frac{\omega_o^2}{2} = \frac{1}{2}\frac{\omega_o^2}{\theta}$$

$$2 = -\frac{1}{2} \frac{33.3^2}{3} = -184 \text{ rev}_{min^2}$$

or
$$\mathcal{L} = -\frac{1}{2} \frac{(0.55)^2}{3} = 0.05 \text{ reV/s}^2 = 0.314 \text{ rad/s}^2$$

b) Let:
$$\theta_0 = 0$$
, $\omega_0 = 0$, $\omega = 33.3 \text{ reV}_{min}$, $t_1 = 3.0 \text{ s}$, $t_2 = 3.5 \text{ min}$

During acceleration

$$\theta_i = 4 \propto t_i^2$$

$$\Rightarrow \theta_i = \lambda \frac{\omega}{x} t_i^x$$

t,=3,Q= = 0.05m

$$\Rightarrow \alpha = \frac{\omega}{t}$$

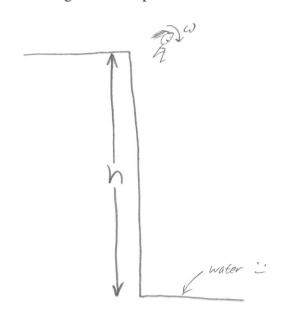
$$\theta_s = \theta_t + \omega_t t_2$$

$$= \partial_s = \omega_i t_i + \omega_i t_s$$

$$= \partial_2 = \omega_i (t_2 + t_2)$$

$$\theta_{a} = 117 \text{ revolutions}$$

A diver makes 2.5 complete revolutions on the way from a 10 m high platform to the water. Assume that her initial vertical velocity was zero. What was her angular velocity, assuming that it was constant throughout the trip.



$$\theta = 2.5 \text{ rev.}$$
 $\omega_0 = ?$

$$h = 10 \text{ m}$$

$$V = 0$$

$$\alpha = 0$$

Rotation
$$\partial = \theta_0 + W_0 t + \sqrt{2} t^2$$

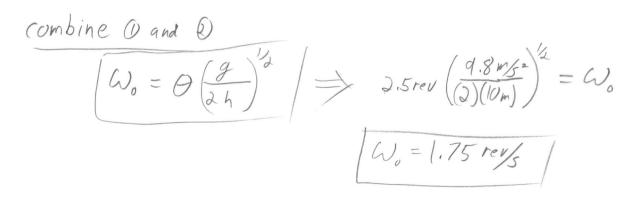
$$\theta = W_0 t$$

$$= \sqrt{W_0} = \frac{\theta}{t} = 0$$

$$\frac{translation}{y = y_0 + y_0 + t} + y_0 + t^2$$

$$0 = h - y_0 + y_0 + t^2$$

$$\Rightarrow \left[t = \left(\frac{2h}{g} \right)^{1/2} \right] = 0$$



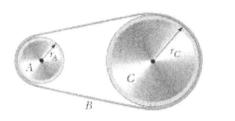
Rotation - Set 1

A wheel with a radius r=0.1 m rolls in a straight line without slipping along a flat floor. When the center of the wheel is at x=0 m, it's linear speed is 2 m/s. The wheel decelerates at a constant rate and stops when its center is at x=5 m.

- (a) Through what angle, in radians, has the wheel rotated?
- (b) What is the wheel's initial angular velocity?
- (c) What is the wheel's angular acceleration, α , over this path?

a)
$$d = r\theta$$
 $\Rightarrow \theta = \frac{d}{r} = \frac{5m}{0.1m} = \frac{50 \text{ radians}}{1 = 0.1m} = \frac{5m}{0.1m} = \frac{50 \text{ radians}}{1 = 0.1m} = \frac{3ms}{0.1m} = \frac{3ms}{0$

A pulley of radius $r_A = 10$ cm is coupled by a belt to a pulley of radius $r_C = 25$ cm. A motor is attached to the axle of pulley A giving it an angular acceleration of $\alpha_A = 1.6$ rad/s². How long does it take pulley C to achieve an angular velocity of 100 rev/min assuming that the belt does not slip?



L=1.6 rads We = 100 rev 211 rev 605

We need to relate x_c to x_A .

Because they are coupled by the belt, a point on the rim of A must have the same linear acceleration as a point on the rim of C.

So,
$$\Gamma_A \mathcal{A}_A = \Gamma_C \mathcal{A}_C = \mathcal{A}_C = \frac{\Gamma_A}{\Gamma_C} \mathcal{A}_A$$

Now, using kinematics:

$$\omega = \omega_0^2 + \lambda t = \omega_0 = \lambda_0 t$$

$$= \lambda_0 + \lambda t = \omega_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 t = \omega_0 \cdot \frac{r_c}{\lambda_A}$$

$$= \lambda_0 + \lambda_0 \cdot \frac{r_c}{\lambda_A}$$

Rotation - Set 1

8 4

A car's odometer works by counting the revolutions of the axle. A car's speedometer works by measuring the angular velocity of the axle. For the odometer and speedometer to work correctly, the correct tire radius has to be set at the factory.

My car came from the factory with tires with a diameter of $d_1 = 60$ cm. They wore out and I replaced them with tires with a diameter of $d_2 = 80$ cm.

- a) With the proper tires on the car, What is the angular displacement of the tire after 1.0 km in radians and in revolutions? What is the angular velocity of the axle if I'm driving 100 km/hr in rad/s and in rev/s?
- b) What are the answers to the questions in part a with the improper tires on the car?
- c) If I've added 10,000 miles to the odometer since putting the new tires on, how many miles have I actually driven the car? (HINT: The odometer *assumes* that the proper tires are on the car.)
- d) If the speed limit is 65 mph, what should my speedometer read so that I don't get a speeding ticket? (HINT: The speedometer *assumes* that the proper tires are on the car.)

a)
$$S = r\theta \Rightarrow \theta = \frac{S}{r}$$

$$S = 1.0 \text{ km}$$

$$C = \frac{1.0 \text{ km}}{6.0 \times 10^{-4} \text{ km}} = \left[1.7 \times 10^{3} \text{ radian s} \right]$$

$$= \left[1.7 \times 10^{3} \text{ rad} \cdot \frac{1}{317} \frac{\text{rev}}{\text{rad}} \right]$$

$$= \left[3.7 \times 10^{3} \text{ rad} \cdot \frac{1}{317} \frac{\text{rev}}{\text{rad}} \right]$$

$$= \left[3.7 \times 10^{3} \text{ rad} \cdot \frac{1}{317} \frac{\text{rev}}{\text{rad}} \right]$$

$$= \left[3.8 \times 10^{-3} \text{ km/s} \right]$$

$$W = \frac{3.8 \times 10^{-3} \text{ km/s}}{6.0 \times 10^{-4} \text{ km}} = \left[4.7 \times 10^{-4} \text{ km/s} \right]$$

$$W = \frac{3.8 \times 10^{-3} \text{ km/s}}{6.0 \times 10^{-4} \text{ km}} = \left[4.7 \times 10^{-4} \text{ km/s} \right]$$

$$W = \frac{3.8 \times 10^{-3} \text{ km/s}}{6.0 \times 10^{-4} \text{ km}} = \left[4.7 \times 10^{-4} \text{ km/s} \right]$$

$$W = 4.7 \text{ rad/s} \cdot \frac{1}{3.77 \text{ rad/s}} = \left[7.5 \text{ rev/s} \right]$$

UST Physics, A. Green, M. Johnston and G. Ruch

Rotation Set 1, Pa continued.

$$\theta = \frac{1.0 \, \text{km}}{8.0 \times 10^{-4} \, \text{km}} = 1250 \, \text{radians}$$

$$\omega = \frac{2.8 \times 10^{-2} \, \text{km}}{8.0 \times 10^{-4} \, \text{km}} = 35 \, \text{rad/s}$$

$$\omega = \frac{35 \text{ rad}_s}{217 \text{ rad/s}} = 5.6 \text{ rev/s}$$

c) The odometer assumes
$$r=d$$
, and displays:

$$\sigma S_0 = d, \theta$$
, $\theta = axle \ rotation \ in \ radians$
 $S_0 = Odometer \ reading$

In reality, the distance traveled by the car is given by:

$$\frac{S_R}{S_0} = \frac{d_2 R}{d_1 R} = \int S_R = \frac{80}{60} |0,000| = [13,333] \text{ miles}$$
Continued 1

Rotation Set 1 PB continued

d) The argument is similar to part c:

The speedometer assumes n=d, and displays:

0
$$V_0 = d, \omega$$
 $\omega = angular \ velocity \ of axle in rad;$
 $V_0 = Speedometer \ reading$

In reality, the velocity of the car is given by: $\mathcal{O} V_R = d_s W \qquad \omega = \text{angular Velocity of the ande in rad}_s$ $\mathcal{V}_R = \text{actual speed of car.}$

W is common so dividing & yields:

$$\frac{V_0}{V_R} = \frac{d_1 \mathcal{X}}{d_2 \mathcal{X}} \Longrightarrow \left[V_0 = \frac{d_1}{d_2} V_R \right]$$

so when 1/2 = 65 mi/hr:

Rotation, moment of inertia

A wagon wheel with a radius of R=30cm with 8 equally spaced spokes is spinning with an angular velocity of ω =2.5 revolutions/sec. You want to shoot a 20 cm arrow parallel to the wheel's axle between the spokes without hitting one. Assuming that the spokes and the arrow are very thin:

a) What minimum speed must the arrow have?

b) Does it matter where between the axle and the rim you aim? If so, where is the best location?



Circle is 271 radians.

There are 8 equal wedges:

$$at: \theta = \frac{2\pi}{8} = \frac{11}{4} each$$

Let's consider that we aim the arrow a distance of above the axle. If it just misses a spoke, It has to be all the way through bofore the next spoke gets there.

The spoke is moving at V= rw
and hasto travel adistance 5= ro

$$S = Vt = P R\theta = R\omega t$$

 $\theta = \omega t \Rightarrow time is independent$
 $0 \in r$. continued f

50: $t = \frac{\theta}{\omega}$ So, the arrow travels it's longth in $l = Vt = V\frac{\theta}{\omega}$

50 It has to go

 $\left(\mathcal{V} = l \frac{\omega}{\theta} \right)$

V = 20 cm = 25 00/3 - 274 rad

V=(2)(25)(20) CM/5 = 100 cm/5